

$$\begin{aligned}
a) \quad & \overline{\overline{ABC} \vee D} \vee \overline{\overline{ACD} \vee B} = \overline{\overline{ABC} \vee D} \overline{\overline{ACD} \vee B} = \\
& = (ABC \vee D)(\overline{ACD} \vee B) = (ABC \vee D)(\overline{A} \vee \overline{C} \vee \overline{D} \vee B) = \\
& = A\overline{ABC} \vee AB\overline{C} \vee ABC\overline{D} \vee ABBC \vee \overline{AD} \vee \overline{CD} \vee \overline{DD} \vee BD = \\
& = 0 \vee 0 \vee ABC\overline{D} \vee ABC \vee \overline{AD} \vee \overline{CD} \vee 0 \vee BD = ABC \vee \overline{AD} \vee \overline{CD} \vee BD = \\
& = ABC \vee \overline{AD} \vee \overline{CD} \vee BD(A \vee \overline{A})(C \vee \overline{C}) = \\
& = ABC \vee \overline{AD} \vee \overline{CD} \vee ABCD \vee AB\overline{CD} \vee \overline{ABCD} \vee \overline{ABC}\overline{D} = \\
& = (ABC \vee ABCD) \vee (\overline{AD} \vee \overline{ABCD} \vee \overline{ABC}\overline{D}) \vee (\overline{CD} \vee ABC\overline{D}) \\
& = ABC \vee \overline{AD} \vee \overline{CD} = ABC \vee (\overline{A} \vee \overline{C})D
\end{aligned}$$

U ovom zadatku lako se dolazi do izraza  $ABC \vee \overline{AD} \vee \overline{CD} \vee BD$ , nakon čega se član  $BD$  može eliminirati kao u Primjeru 6.9 u udžbeniku, ili ovako kako je demonstrirano ovdje, dvostrukim proširenjem tog člana i apsorpcijom dijelova dobijenih nakon proširenja u druge članove.

$$\begin{aligned}
b) \quad & \overline{\overline{ABC} \vee \overline{D}} \vee \overline{\overline{ACD} \vee B} = \overline{\overline{ABC} \vee \overline{D}} \overline{\overline{ACD} \vee B} = \\
& = (A\overline{B}\overline{C} \vee \overline{D})(\overline{ACD} \vee B) = (A\overline{B}\overline{C} \vee \overline{D})(\overline{A} \vee \overline{C} \vee \overline{D} \vee B) = \\
& = A\overline{A}\overline{B}\overline{C} \vee A\overline{B}\overline{C}\overline{C} \vee A\overline{B}\overline{C}\overline{D} \vee AB\overline{B}\overline{C} \vee \overline{A}\overline{D} \vee \overline{CD} \vee \overline{DD} \vee \overline{BD} = \\
& = 0 \vee 0 \vee A\overline{B}\overline{C}\overline{D} \vee 0 \vee \overline{A}\overline{D} \vee \overline{CD} \vee \overline{D} \vee \overline{BD} = \\
& = A\overline{B}\overline{C}\overline{D} \vee \overline{A}\overline{D} \vee \overline{CD} \vee \overline{D} \vee \overline{BD} = \overline{D}
\end{aligned}$$

Ovdje se u posljednjem koraku vidi da član  $\overline{D}$  apsorbira u sebe sve ostale članove.

$$\begin{aligned}
c) \quad & \overline{\overline{ABC} \vee D} \vee \overline{\overline{ACD} \vee \overline{B}} = \overline{\overline{ABC} \vee D} \overline{\overline{ACD} \vee \overline{B}} = \\
& = (A\overline{B}\overline{C} \vee D)(\overline{ACD} \vee \overline{B}) = A\overline{A}\overline{B}\overline{C}\overline{D} \vee A\overline{B}\overline{B}\overline{C} \vee \overline{ACDD} \vee \overline{BD} = \\
& = 0 \vee A\overline{B}\overline{C} \vee \overline{ACD} \vee \overline{BD} = A\overline{B}\overline{C} \vee \overline{ACD} \vee \overline{BD} = A\overline{B}\overline{C} \vee (\overline{AC} \vee \overline{B})D \\
d) \quad & \overline{\overline{AB} \vee \overline{CD}} \vee \overline{\overline{AC} \vee \overline{BD}} = \overline{\overline{AB} \vee \overline{CD}} \overline{\overline{AC} \vee \overline{BD}} = \\
& = (A\overline{B} \vee \overline{CD})(\overline{AC} \vee \overline{BD}) = A\overline{A}\overline{B}\overline{C} \vee A\overline{B}\overline{B}\overline{D} \vee \overline{ACCD} \vee \overline{BCDD} = \\
& = 0 \vee A\overline{B}\overline{D} \vee 0 \vee \overline{B}\overline{CD} = A\overline{B}\overline{D} \vee \overline{B}\overline{CD} = \overline{BD}(A \vee \overline{C})
\end{aligned}$$